## Math 200 - 1st Final Exam

December 1, 2010

Name \_\_\_\_\_\_\_

Show all work to receive full credit. Supply explanations where necessary. Multiple choice problems are worth 0, 1, or 2 points depending on your answer and the work shown.

- 1. When using the 4-step, problem-solving process which one of these strategies would NOT be considered part of devising a plan?
  - (a) Look for a pattern.
  - (b) Sketch a picture.
  - (c) Examine a smaller problem.
  - (d) Determine what information is irrelevant.
- 2. Choose the subtraction model that best fits the following problem situation: Caleb has 5 cookies and Katie has 3 cookies. How many more cookies does Caleb have?
  - (a) comparison
  - (b) take away
  - (c) number line
  - (d) missing addend
- 3. Use any appropriate addition algorithm to compute the following sum.

$$33_{\text{four}} + 22_{\text{four}} + 32_{\text{four}} + 1_{\text{four}} + 20_{\text{four}} + 3_{\text{four}} + 13_{\text{four}}$$

- (a)  $124_{\text{four}}$
- (b) 130<sub>four</sub>
- (c) 322<sub>four</sub>
- (d)  $333_{\text{four}}$
- 4. Which one of the following facts demonstrates the associative property of addition?
  - (a) 2(5+1)+3=2(1+5)+3
  - (b) (6x+10) = 2(3x+5)
  - (c) (x+3) + (2+y) = (y+2) + (x+3)
  - (d) (4+1)+2=4+(1+2)

5.	Which one	of	the	following	is	not	a	basic	property	of	the	${\bf Hindu-Arabic}$	numeration	on
	system?													

- (a) Place value is based on powers of 10.
- (b) Each digit in a numeral has a face value, a place value, and a value.
- (c) Each number is either prime or composite.
- (d) All numerals are constructed from the 10 digits.
- 6. Consider the following conjecture:

If 
$$3 \mid x$$
, then  $6 \mid x$ .

Which one of the following is a counterexample?

- (a) 3 | 18 and 6 | 18.
- (b)  $3 \nmid 10 \text{ and } 6 \nmid 10$
- (c)  $3 \mid 27 \text{ and } 6 \nmid 27$
- (d) The conjecture is true.
- 7. The prime factorization of a number is  $2^5 \cdot 3^3 \cdot 5$ . How many positive integer divisors does the number have?
  - (a) 15
  - (b) 48
  - (c) 64
  - (d) 24
- 8. Which one of these numbers is the 835th term of the following arithmetic sequence?

$$10, 13, 16, 19, 22, 25, \dots$$

- (a) 2512
- (b) 2518
- (c) 2515
- (d) 2524
- 9. Which one of the following is an example of deductive reasoning?
  - (a) Every elephant I have ever seen is gray. Therefore every elephant must be gray.
  - (b) It has rained every day. Therefore it will rain tomorrow.
  - (c) Since multiplication is commutative,  $15 \cdot 37$  must be equal to  $37 \cdot 15$ .
  - (d) A sequence begins with 1,2,3,4. The next term must be 5.

- 10. Choose the division model that best fits the following problem situation: 52 playing cards are shared equally among 4 people. How many cards does each person get?
  - (a) partition
  - (b) missing factor
  - (c) repeated subtraction
  - (d) division algorithm
- 11. Let  $A = \{0, 1, 2, 3\}$ . Choose the set B for which all of the following are true?

$$4 \in B$$
,  $A \sim B$ ,  $A \cap B = \emptyset$ ,  $(7,2) \in B \times A$ 

- (a)  $B = \{4, 7\}$
- (b)  $B = \{4, 5, 7, 8\}$
- (c)  $B = \{3.5, 4, 8, 9\}$
- (d)  $B = \{0, 2, 4, 7\}$
- 12. Convert  $4103_{six}$  to base ten.
  - (a) 5403
  - (b) 903
  - (c) 5418
  - (d) 3555
- 13. (5 points) In the harbor there were ships with 3 masts and ships with 4 masts. John saw 7 ships and counted a total of 26 masts. How many ships had 3 masts and how many had 4? (Use any technique to solve the problem, but show your work or explain your reasoning. You will receive no credit for simply writing a answer.)

14. (1 point) Give an example of a geometric sequence.

15. (5 points) Clearly state the rule for adding two integers with opposite signs. Give an example that illustrates your rule.

16. (5 points) Use a model to illustrate each of the following. (Model what is given, not a related problem.)

(a) 
$$-5+3$$

(b) 
$$(-3) \times (-4)$$

(c) 
$$-3 - (-7)$$

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- 18. (5 points) Let  $A = \{1, 2, 3\}$  and  $B = \{x, y\}$ .
  - (a) Find the Cartesian product  $A \times B$ .

(b) Write a word problem involving the multiplication fact  $3 \times 2 = 6$  that is most naturally modeled using the Cartesian product model.

- 19. (5 points) Classify each of the following as true or false. If false, provide a counterexample.
  - (a) If n(A) = n(B), then A = B.
  - (b) If  $A B = \emptyset$ , then A = B.
  - (c) If  $A \subseteq B$ , then  $A \cap B = A$ .

20. (5 points) In a survey of 393 horticulturists, the following information was obtained:							
• 231 keep orchids;							
• 220 keep cacti;							

- 165 keep African violets and orchids;
- $\bullet\,$  151 keep African violets and cacti;
- 142 keep orchids and cacti;
- 115 keep all three types of plants; and
- 12 keep none of these types of plants.

Organize the data in a three-set Venn diagram. How many people surveyed keep only African violets?

21. (5 points) Find digits s and t so that 1s52t is divisible by 12, and 1s52t has the greatest possible value. Once you've found your number, also test it for divisibility by 8 and 9.

22.		oints) State the four steps of the 4-step, problem-solving process. Choose any one our steps (Tell which you choose!) and list two strategies associated with that step.
23.	(5 pc	oints)
	(a)	What does it mean for a positive integer to be prime?
	(b)	When testing to determine whether 1073 is prime, what is the greatest prime that must be checked?
	(c)	Determine whether $1073$ is prime. If it is not prime, determine its prime factorization.
	(d)	What does it mean for a positive integer to be composite?