

**Math 129 - Test 3**

November 19, 2020

Name \_\_\_\_\_

Score \_\_\_\_\_

**Show all work to receive full credit.** Supply explanations where necessary. Label your axes when graphing. You may get partial credit on multiple choice problems if you show correct work or explanations.

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1. (6 points [5]) The functions  $f$  and  $g$  are defined in the table shown below. Use the data from the table to evaluate each of the following.

$x$	1	2	3	4	5
$f(x)$	-1	3	2	5	0
$g(x)$	7	0	4	-7	4

(a)  $(g + f)(3)$

(b)  $(gg)(4)$

(c)  $\left(\frac{g}{f}\right)(0)$

(d)  $(f \circ g)(5)$

2. (4 points [5]) Refer to the functions  $f$  and  $g$  defined in the problem above.

(a) What is the domain of  $(g \circ f)$ ?

(b) What is the range of  $(g \circ f)$ ?

3. (4 points [5]) The formula for the surface area ( $S$ ) of a sphere of radius  $r$  is  $S = 4\pi r^2$ . A spherical balloon is being inflated in such a way that its radius (in inches) after  $t$  minutes is given by  $r(t) = 3t + 1$ . Find a formula for  $S$  in terms of the time  $t$ . Completely expand and simplify your answer.

4. (6 points [1,5]) Consider the function

$$f(x) = \begin{cases} x^2 + x, & x < -5 \\ |x + 6| + 2, & -5 \leq x < 1 \\ \sqrt{6x}, & x > 2 \end{cases}$$

(a) Evaluate  $f(6)$ .

(b) Evaluate  $f(-10)$ .

(c) Evaluate  $f(1)$

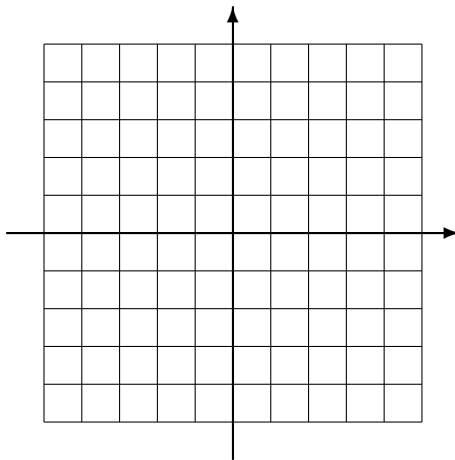
(d) What is the domain of  $f$ ?

5. (8 points [1,5,9]) Consider the function

$$f(x) = \begin{cases} -x + 2, & x < 0 \\ x^2, & x \geq 0 \end{cases}$$

(a) What is the domain of  $f$ ?

(b) Carefully sketch the graph of  $f$ . Label your axes.



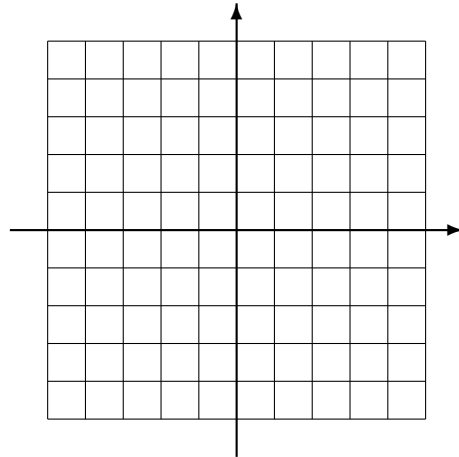
(c) Is  $f$  a continuous function? If not, where is it discontinuous?

6. (4 points [9]) Determine the equations of the horizontal and vertical asymptotes of the graph of  $y = \frac{1}{x+6} - 8$ . (Hint: Think about how the graph is related to that of  $y = 1/x$ .)

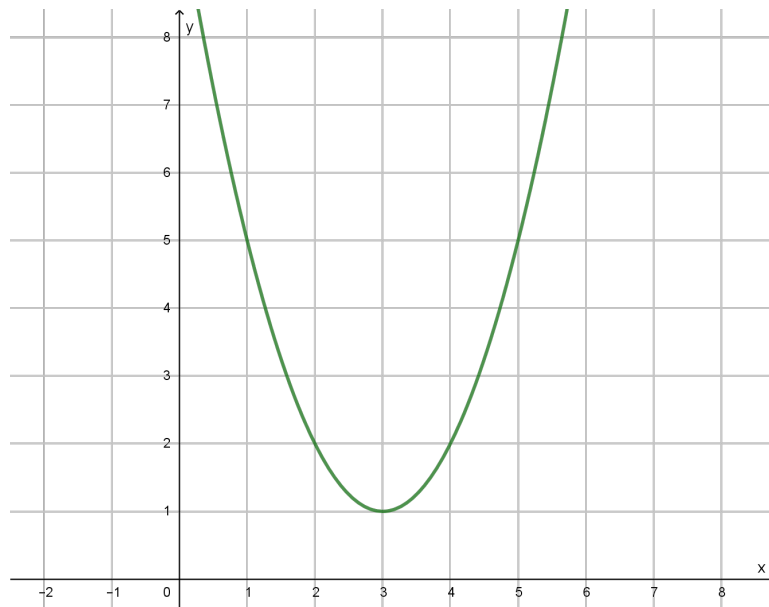
7. (3 points) Find two functions  $f$  and  $g$  so that  $(f \circ g)(x) = (2 + \sqrt{x})^5$ .

8. (6 points [9]) What are the domain and range of the function  $g(x) = 6 + \sqrt{x - 3}$ ? Write your answers in interval notation, and say which answer is which.

9. (7 points [9]) Explain how the graph of  $g(x) = \frac{1}{2}|x + 1|$  can be obtained from the graph of  $g(x) = |x|$ . Then carefully sketch the graph of  $g$ . (Label your axes.)

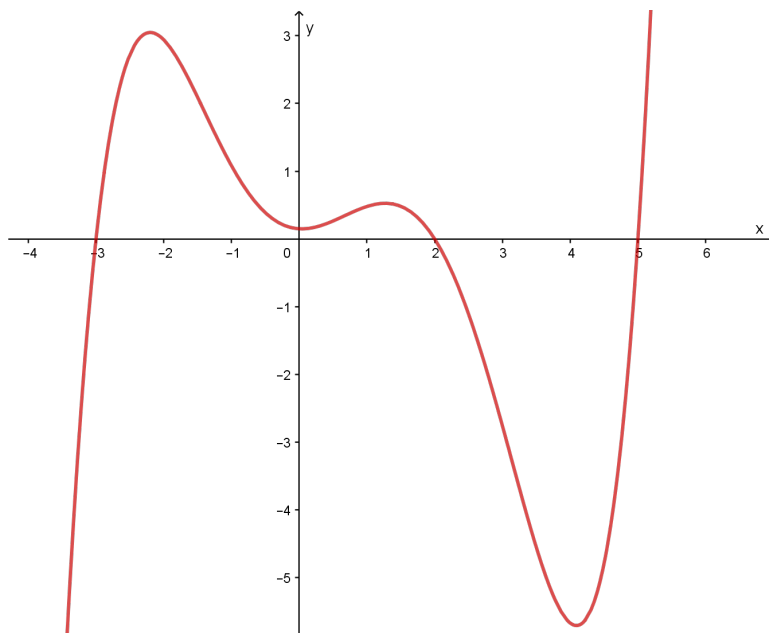


10. (3 points [9]) The graph of  $y = x^2$  is shifted to obtain the new graph shown below. What is an equation for the new graph?



11. (8 points [5]) Let  $f(x) = \frac{5}{x+3}$  and  $g(x) = \frac{6}{x-7}$ . Determine the domain of the function  $(f \circ g)$ .

12. (9 points [8,10]) The graph of the function  $f$  is shown below.



- (a) Determine the intervals on which  $f(x) > 0$ .
- (b) Determine the intervals on which  $f$  is decreasing.
- (c) Determine any relative (local) minimum or maximum values. Say which are which.

13. (18 points [8,10]) Consider the following types of functions:

**A** – Constant functions,  $f(x) = c$

**B** – Linear functions (Not constant),  $f(x) = mx + b$ ,  $m \neq 0$

**C** – Absolute value function,  $f(x) = |x|$

**D** – Reciprocal function,  $f(x) = 1/x$

**E** – Reciprocal square function,  $f(x) = 1/x^2$

**F** – Squaring function,  $f(x) = x^2$

**G** – Square root function,  $f(x) = \sqrt{x}$

**H** – Cubing function,  $f(x) = x^3$

**I** – Cube root function,  $f(x) = \sqrt[3]{x}$

For each part below, indicate (by letter) which functions have the given property. List all that apply.

(a) The graph has a U shape.

(b) The  $x$ -axis is a horizontal asymptote of the graph.

(c) The graph is symmetric about the origin.

(d) The graph is a line.

(e) The domain is the set of all real numbers.

(f) The graph has V shape.

(g) The graph is symmetric about the  $y$ -axis.

(h) The graph has a vertical asymptote.

(i) The range is the set of real numbers.

14. (2 points [8,10]) Which one of the following properties would indicate that the graph of  $f$  is symmetric about the origin?
- (a)  $(f/f)(x) = f(x)$
  - (b)  $f(-x) = -f(x)$
  - (c)  $f(-x) = f(x)$
  - (d)  $f(x) = (f \circ f)(-x)$
15. (2 points [8,10]) Which one of the following properties would indicate that the graph of  $f$  is symmetric about the  $y$ -axis?
- (a)  $f(-x) = -f(x)$
  - (b)  $f(-x) = -f(-x)$
  - (c)  $f(x) = (f \circ f)(x)$
  - (d)  $f(-x) = f(x)$
16. (2 points [8,10]) Which function has a graph that is symmetric about the  $x$ -axis?
- (a)  $f(x) = \frac{1}{x-2} + 193$
  - (b)  $g(x) = 63\sqrt[3]{x-4}$
  - (c)  $h(x) = 5x^2 + 55x + 555$
  - (d) No such function exists.
17. (2 points [8,10]) Which function has a graph that is symmetric about the origin?
- (a)  $h(x) = 0.000001x^2$
  - (b)  $g(x) = 0.000001\sqrt{x}$
  - (c)  $f(x) = 0.000001x^3$
  - (d) No such function exists.
18. (2 points [8,10]) Which function has a graph that is symmetric about the  $y$ -axis?
- (a)  $g(x) = 0.0000001x^3$
  - (b)  $f(x) = 8723 - 5135x^2$
  - (c)  $h(x) = \frac{829}{x-517}$
  - (d) No such function exists.

19. (2 points [8,10]) True or False: A local (relative) maximum value of a function must be greater than a local minimum.
20. (2 points [8,10]) Suppose you are given the graph of a function  $f$ , and you would like to solve the inequality  $f(x) > 0$ . Which of the following should you do?
- (a) Identify the portions of the  $x$ -axis where the graph is lying below the axis.
  - (b) Identify the portions of the  $x$ -axis where the graph is lying above the axis.
  - (c) Identify the portions of the  $x$ -axis where the graph is falling to the right.
  - (d) Identify the portions of the  $x$ -axis where the graph is rising to the right.